Biophysics Lecture Tuesday, April 9th, 2019

Presenter: Emre Brookes

Topic: Small Angle Scattering - III

Copy of Lecture at:

https://demeler.uleth.ca/biophysics/archive/Brookes

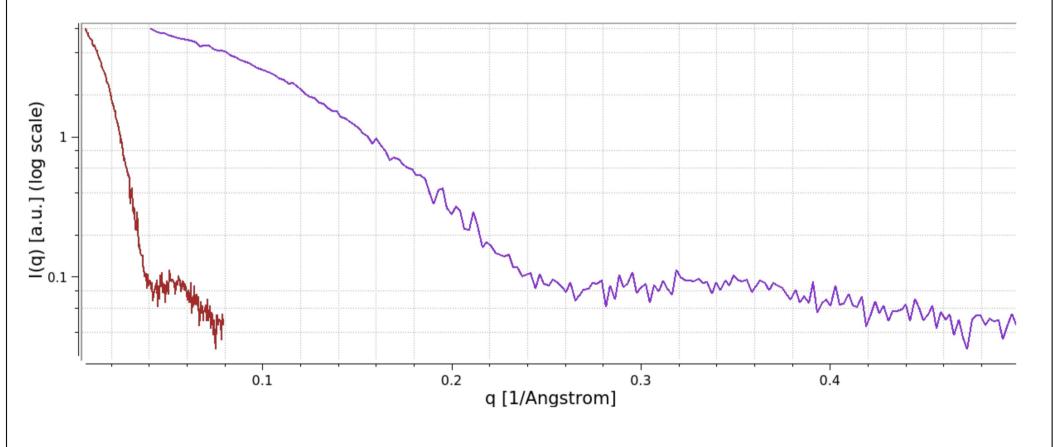
Outline

- Homework answers
- Brief review
- Practical considerations
- Sampling of other techniques

1. The dimensionless Kratky plot shows a peak of \sim (1.75,1.1) for globular proteins. Would this peak change if the experimental data had a momentum

transfer of
$$s = \frac{2\sin(\theta)}{\lambda}$$
? $q = \frac{4\pi\sin(\theta)}{\lambda}$

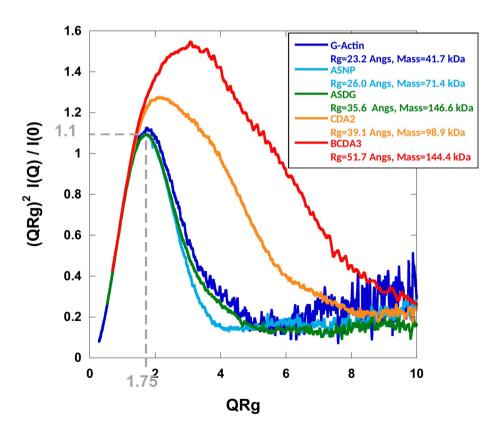
If so, what would be the peak?



1. The dimensionless Kratky plot shows a peak of \sim (1.75,1.1) for globular proteins. Would this peak change if the experimental data had a momentum

transfer of $s = \frac{2\sin(\theta)}{\lambda}$?

If so, what would be the peak?



$$q = \frac{4\pi \sin(\theta)}{\lambda}$$

$$qR_g = 1.75$$

$$2\pi sR_g = 1.75$$

$$sR_g = \frac{1.75}{2\pi} \cong 0.279$$

$$(qR_g)^2 I(q) / I(0) = 1.1$$

$$(2\pi)^2 (sR_g)^2 I(s) / I(0) = 1.1$$

$$(sR_g)^2 I(s) / I(0) = \frac{1.1}{(2\pi)^2} \cong 0.0279$$

$$I(q) \rightarrow I(s)$$
o.w. taking values from another data point that might not exist

Peak: ~(0.279,0,0279)

SAS provides a sensitive means to evaluate *the degree of compactness* of a protein:

- To determine whether a protein is globular, extended or unfolded ٠
- To monitor the folding or unfolding transition of a protein ٠

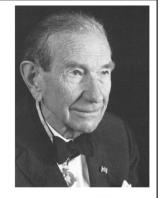
1.0Unfolded $q^2 I(q)$ versus $q \stackrel{(b)}{\underset{cb}{\sim}} 0.5$ Partially unfolded Folded 0.00.00. o.ٰع q [1/Angstrom] 0.1 0.2 0.4

Folded particle : *bell-shaped curve* (asymptotic behavior $I(q) \sim q^{-4}$) Random polymer chain : *plateau* at large q-values (asymptotic behavior $I(q) \sim q^{-2}$) Extended polymer chain : *increase* at large q-values (asymptotic behavior $I(q) \sim q^{-Lx}$)

This is most conveniently represented using the Kratky plot:

l(q) [a.u.] (log scale)

0.1



Prof. Otto Kratky 1902-1995 Graz, Austria

Putnam, D., et al. (2007) Quart. Rev. Biophys. 40, 191-285.

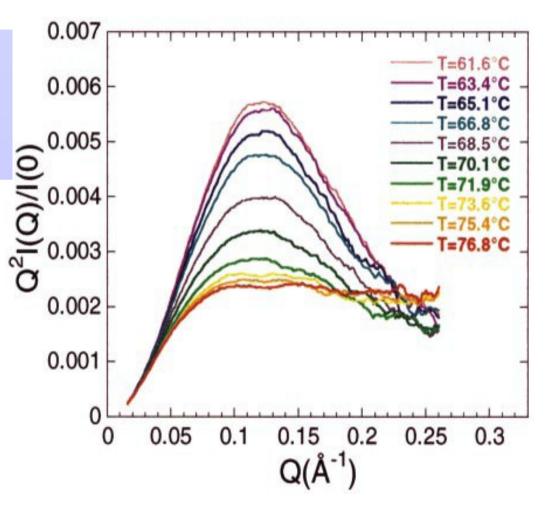
Review – Kratky plots of (partially) folded proteins

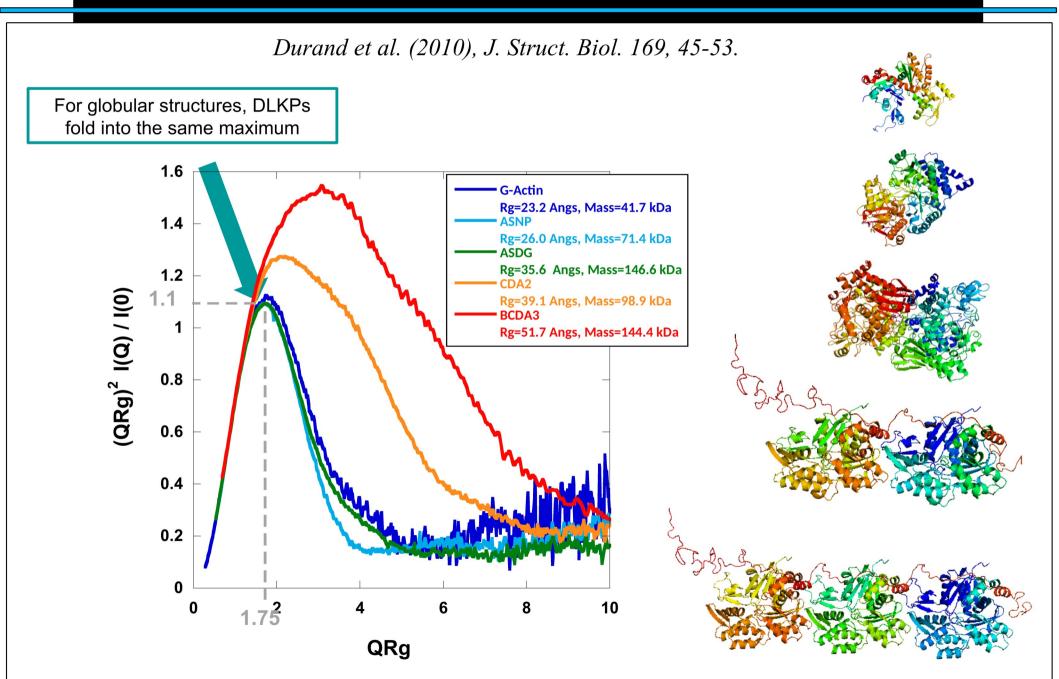
Pérez et al., J. Mol. Biol. (2001), 308, 721-743



In practice, thin Gaussian chains do not exist.

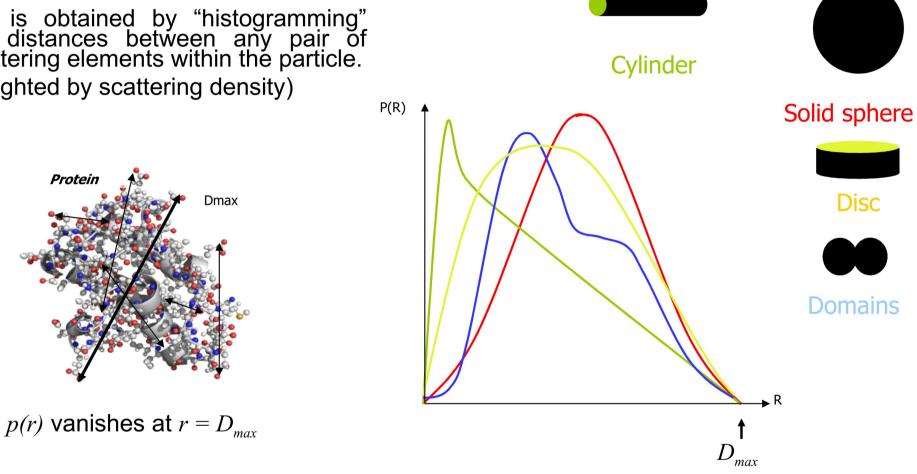
In spite of the plateau at T=76°C, NCS is not a Gaussian chain when unfolded, but a thick chain with persistence length.





The maximum value on the dimensionless bell shape tells if the protein is globular.

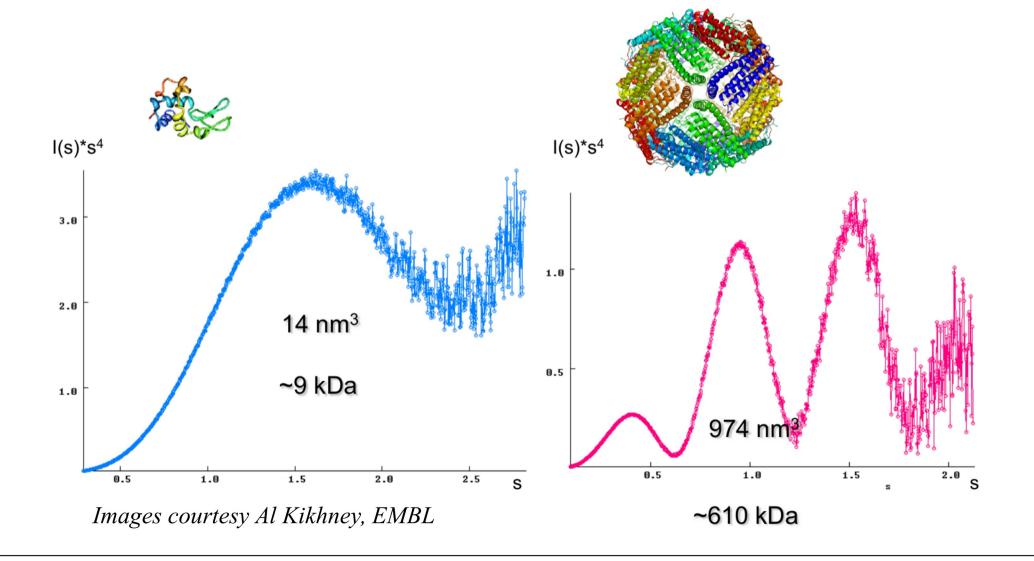
p(r) is obtained by "histogramming" the distances between any pair of scattering elements within the particle. (weighted by scattering density)



The distance distribution function characterizes the shape of the particle in real space

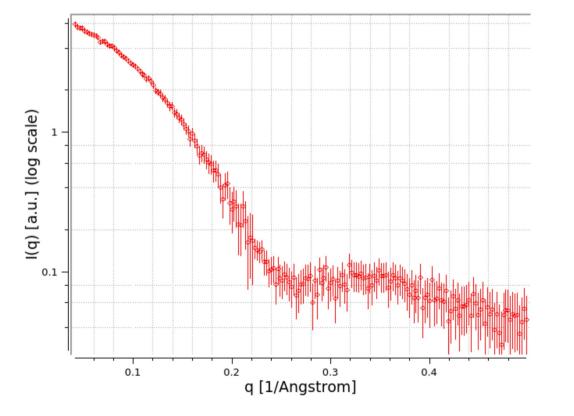
$$V_P = \frac{2\pi^2 I(0)}{\int_0^\infty \left[I(q) - K_4\right] q^2 \, dq}$$

 K_4 is a constant determined to ensure the asymptotic decay of I(q) is proportional to q^{-4}



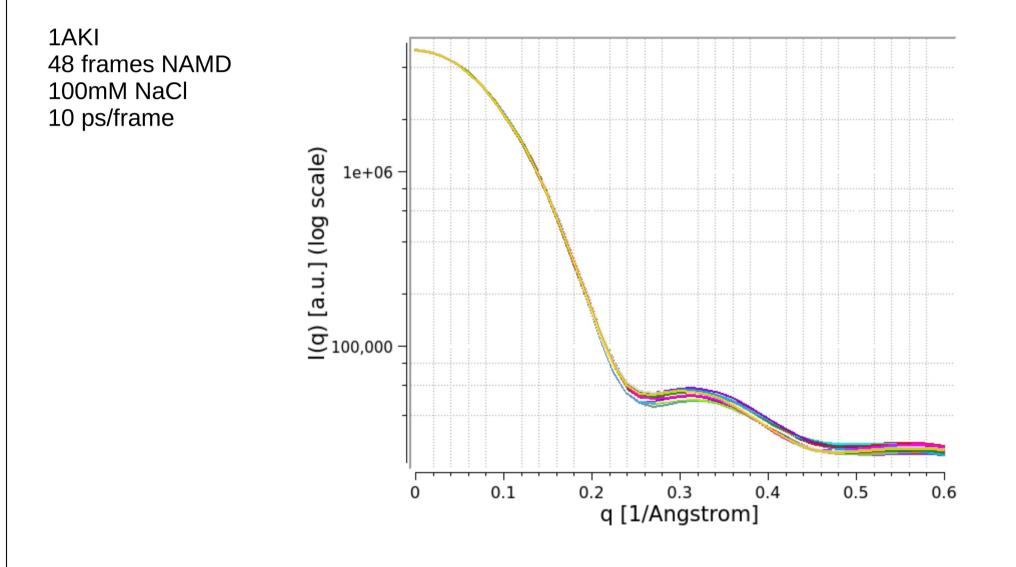
Svergun, D.I. & Koch, M.H.J. (2003) Small-angle scattering studies of biological macromolecules in solution. Rep. Prog. Phys. 66 1735-82

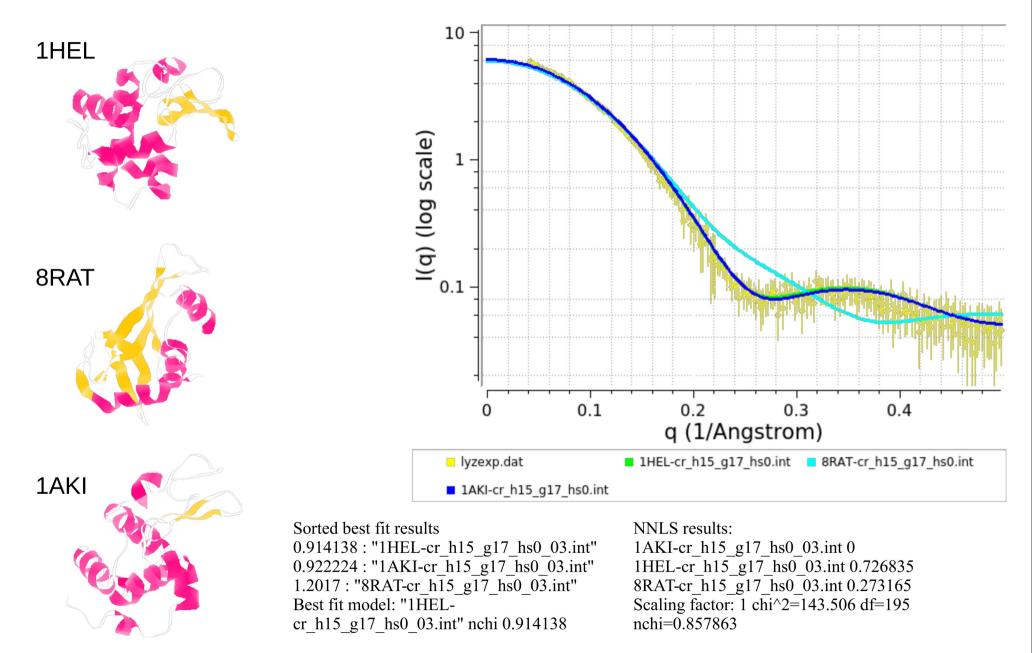
- Shannon channels = $D_{max} \cdot q$ -range / π
- "the number of [obtainable parameters] typically does not exceed 10-15"



Lyzosyme $D_{max} \sim 48$ Angstroms

Shannon channels = 48 * 0.5 / $\pi \sim 8$





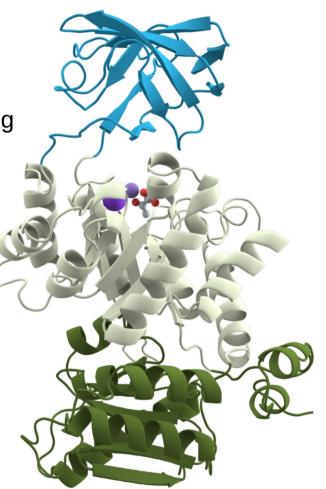
UltraScan-SOMO https://somo.aucsolutions.com

Structure of subunits are known

Arbitrary complex can be constructed by moving and rotating

Verify no steric clashes

- \rightarrow scattering data subunits
- + contacts (chemical shifts by NMR or mutagenesis)+ distances between residues (FRET or mutagenesis)
- + relative orientation (RDC by NMR)



Pyruvate kinase 1PKN

By Thomas Splettstoesser (www.scistyle.com) -Own work, CC BY-SA 3.0

Petoukhov et al. 2006 Eur. Biophys J 35:567

Software for "data reduction", "visualization", "model fitting", various "analysis" ... Grouped packages and stand alone components

ATSAS – Dmitri Svergun group

Scatter – Rob Rambo

BioXTAS Raw – Jesse Hopkins

SASView – multiple contributors

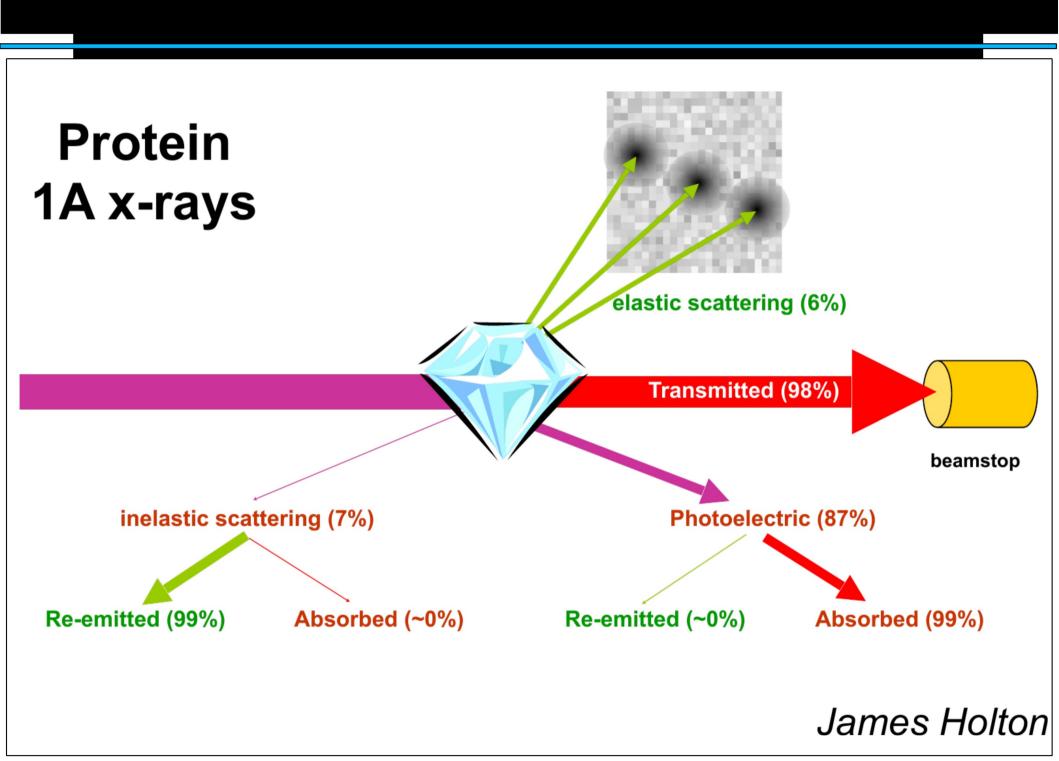
CCP-SAS – SCT/SCTPL / US-SOMO / SASSIE & others – multiple contributors more at *http://smallangle.org/content/software*

Table 1

Incomplete list of methods for predicting SWAXS curves from structural models: Fitting of hydration layer required ($\delta \rho_{fit}$ including method that ignore the hydration layer), using tabulated reduced form factors (f_{red}), resolution [atomistic or coarse grained (CG)], fluctuations included, free availability [Download (D), web server (W)]. Additional software is listed in Refs. [63,64]

ID	Name/authors	Year	$\delta \rho_{\rm fit}/f_{\rm red}$	Resol.	Fluct.	Avail.	Refs.
Implicit	solvent methods						
1	CRYSOL	1995	Yes/yes	atom.	-	D/W	25
2	ORNL-SAS	2007	Yes/yes	atom.	-	D	65
3	SoftWAXS	2009	Yes/-	atom.	-	D	66
4	Fast-SAXS-pro	2009	Yes/yes	CG	Yes	D/W	30,36
5	FoXS	2010	Yes/yes	atom.	-	D/W	67,29
6	PHAISTOS	2010	Yes/yes	CG	-	D	68
7	AquaSAXS/AquaSol	2011	Yes/yes	atom.	-	W	27
8	SASbtx/Zernike	2012	Yes/-	atom.	-	W	69
9	RISM-SAXS	2014	–/yes	atom.	-	D	[70]
10	BCL::SAXS	2015	Yes/yes	atom.	-	D	[71]
11	Pepsi-SAXS	2017	yes/yes	atom.	-	D	72*
Explicit	solvent methods						
12	SASSIM/Sassena	2002	–/yes	atom.	Yes	D	73
13	MD-SAXS	2009	_/_	atom.	Yes	-	74,75
14	AXES	2010	Yes/-	atom.	-	W	[26]
15	HyPred	2011	_/_	atom.	-	W	[76]
16	Park et al.	2009	_/_	atom.	-	-	77
17	Köfinger &Hummer	2013	_/_	atom.	Yes	D	78
18	WAXSIS	2014	_/_	atom.	Yes	D/W	38,79

Table from Jochen S Hub. Curr. Op. in Struct. Bio. 2018, 49:18-26



Sample requirements for (SAXS) solution scattering

- size: >5kD
- purity: highly monodisperse !
- concentration: 0.25 10mg/ml (higher for small proteins and intermediate angle data
- sample volume 15-50 ul ;(so only a fraction of 1mg protein needed for a starting experiment!)
- enough material for at least 3 concentrations
- matching buffer solution is very important (lower salt better)
- most buffer components tolerated (e.g. glycerol (<30%) and salt (<0.5M) are OK)
- S-reducing agent can help protein to stay intact under irradiation

Additional requirements for time-resolved measurements

- lots of sample (at least 10mg, better more)
- sufficiently large change between initial and final state
- pre-characterization of kinetics by other techniques

A good SAXS experiment starts in your home lab

- every protein has it's own "personality"
 - the more you know about your protein the better you can select the data acquisition parameters (buffer composition, pH, additives)
- Characterize your protein as much as possible with biochemical means
 - check for possible oligomerization with concentration
 - in case of complexes: for dissociation under dilution
 - determine highest concentration the protein is stable (and how long?)
 - simulate shipping conditions (e.g. freezing & thawing) and check sample quality afterwards
- know your numbers
 - sequence and MW
 - extinction coefficient and concentration of your stock solution

Practical considerations

Monodispersity

- check your samples:
 - Good solubility (clear solution), no obvious precipitates
 - Single species on native gels
 - SDS-PAGE should show no contamination
 - Single symmetric peak on an SEC column

- Other analytical techniques:
 - Dynamic light scattering (DLS)
 - Analytical ultracentrifugation
 - Mass spectrometry SEC-MALLS

Buffer conditions

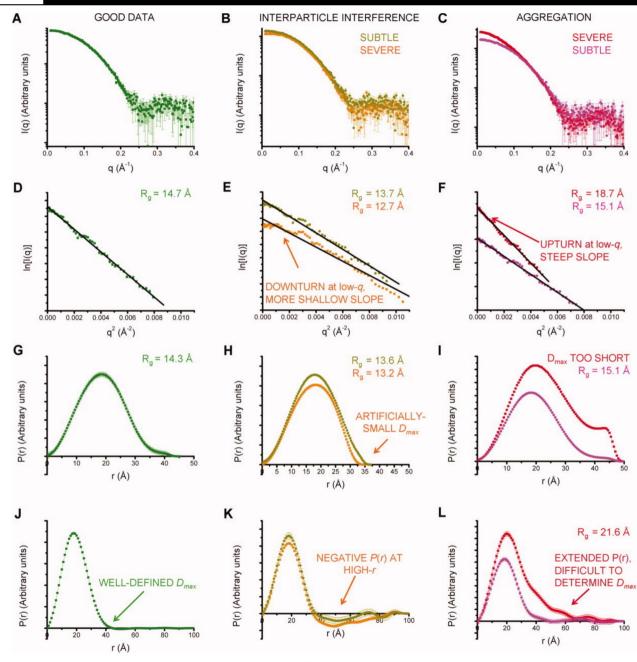
- use a low salt concentration if possible
- for proteins PBS buffer is usually a good choice
- consider additives to prevent radiation damage (DDT, TCEP, Glycerol ...)
- bring plenty of matched buffer

Before coming to SSRL

- provide accurate information in the beamtime request form
- ask beamline staff if you are unsure or have questions
- contact your beamline staff before experiment just in case something changed

At the beamline

- understand how the data collection works and how to load your samples
- take plenty of buffer images
- take advantage of the online data reduction: **monitor what's happening!**
- consider sample recovery for post exposure analysis
- bring additional radical scavengers in case of unexpected radiation damage



Jacques D.A. and Trewhella. Prot. Sci. 2010 19(4):642-657

Immediate data quality checks

- aggregation:
 - upturn at low q
 - residuals in guinier plot will show upward curvature
- interparticle repulsion:
 - downturn at low q
 - residuals in guinier plot will show downward curvature
 - will increase with concentration

Checks with the p(r) function

- determine Dmax
 - no "nose-diving" !
 - no excessive oscillation around 0
 - rule of thumb: $Dmax \approx 3^* Rg$
 - Switch off P(dmax)=0 and use large Dmax to estimate
- determine Rg
 - should compare well with Rg from Guinier

What if your Sample is Aggregated?

- centrifuge your sample (ideally keep it cold)
- dilute and centrifuge
- filter
- add more DTT if radiation damage is the problem
- run sample through SEC column if time permits
- change buffer condition (if you have enough material)



Light sources of the world

There are more than 50 light sources in the world (operational, or under construction). This page lists all the members of the lightsources.org collaboration.



Vorange pins on the map represent members of the lightsources.org collaboration.



Steps are generally the same:

- Find a beamline
- Talk with a beamline scientist
- Register and submit a proposal
- If you are going to do the experiment yourself
 - Safety training etc.



Advanced Photon Source

An Office of Science National User Facility

All About Proposals

Users Home

Apply for Beam Time Deadlines Proposal Types Concepts, Definitions, and Help

My APS Portal



Apply for Beam Time

Next Proposal Deadline

- The proposal submission deadline for Run 2019-3 is Friday, July 5, 2019, at 11:59 p.m. (Chicago time).
- Questions: write to gu_program@aps.anl.gov or call 630-252-9090.
- Please note that Chrome is not supported for the on-line proposal system.

Log in to Proposal System



APS Contact Information

General Inquiries

apsuser@anl.gov (630) 252-9090 8:00 am - 5:00 pm, Monday-Friday

Floor Coordinator on Duty

630-252-0101 (on-call pager) From on-site phone: 2-0101

Main Control Room 630-252-9424

Safety Manager Paul Rossi I If you are awarded time

- Bring a **TEAM!**
- Bring extra samples (ask colleagues).
- Expect to work every hour of your allocation!
 - e.g. if you have 2 days beamtime scheduled, expect to have someone working at the beamline 48 hours



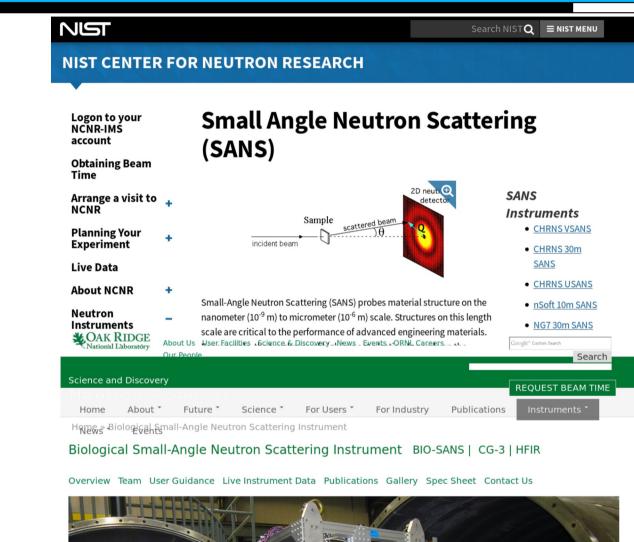


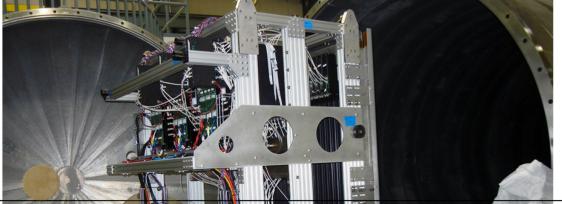
APS at Argonne National Laboratory



SANS beamlines

NCNR, NIST, Maryland HFIR, ORNL, Tennessee ISIS, RAL, UK ILL, Grenoble, France ANSTO, Sydney, Australia ESS, Lund, Sweden (2025) others...





	SAXS	SANS
Features	msec resolution for time- resolved measurements	D labeling and H/D contrast variation
	Superior q-resolution	Magnetic scattering
	Anomalous scattering (ASAXS)	Conducive to extreme environments
	Small sample size	Nondestructive
Complications	Radiation damage to some samples	Incoherent scattering
	Parasitic scattering	H/D isotope effects
	Fluorescence	
	Beam stability	

Charles Glinka, NIST

Anomalous SAXS: Allows limited contrast variation when the adsorption edge of one of the constituent elements is at an accessible energy range.

Theory pioneered by Heinrich B. Stuhrmann: Q. Rev. Biophys. 14, 433 (1981) Adv. Polym. Sci. 67, 123 (1985)

Heinrich B Stuhrmann Guinier prize 2006

Stuhrmann analyzed metal containing proteins such as hemoglobin, ferritin, and the anomalous effect on the radius of gyration of DNA near the absorption edge of counterions.

In the case of the large subunit of ribosome (1500 kD), measurements near phosphorous K-edge allowed separation of all three partial intensities. *Stuhrmann. J. Appl. Cryst. 2007.* 40:s23

M. Sztucki et al., 2012 Eur. Phys J. Special Topics. 208:319-331

Stuhrmann 1981: f" via absorption vs wavelength for bound iron. f" via f" using the Kramers-Kroning relation... Tabulated values are available for most elements. Corrected I(q) curves were produced, compared. Multipole expansion for scattering density \rightarrow distance distributions for iron were estimated.

Generalized in V.J. Pinfield and D.J. Scott. PLoS ONE. 2014 9(4): e95664

Table 2. Distances between label atoms or nanocrystals.

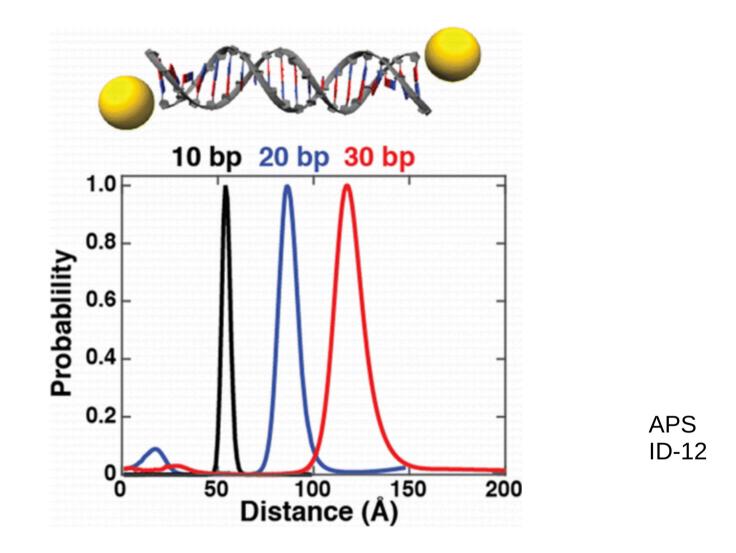
Molecule	Actual distance between labels/Å	Calculated distance between labels/Å
10 bp DNA, atom labels	37.3	
10 bp DNA, nanocrystal	50.5	51
20 bp DNA, nanocrystal	60.7	61
50 bp DNA, nanocrystal	142.0	143
100 bp DNA, nanocrystal	269.6	270
200 bp DNA, nanocrystal	672.0	673

 $f(\lambda) = f_0 + f'(\lambda) + \mathbf{i}f''(\lambda)$

 $|f| = [(f_0 + f')^2 + f''^2]^{\frac{1}{2}}$

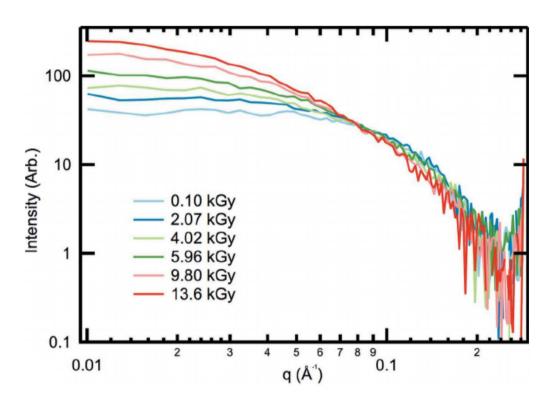
The distance between the label atoms or nanocrystals, as defined in the coordinate files, and determined by the anomalous SAXS simulation. doi:10.1371/journal.pone.0095664.t002

KK: Re/Im of Fourier 1-1 Even odd



Thomas Zettl et al. Nano Letters 2016 16 (9), 5353-5357

X-ray-induced radiation damage can cause macro- molecule aggregation, fragmentation, conformation changes and unfolding, all of which can be detected by SAXS. Radiation damage is therefore a major obstacle for SAXS, and descriptions of dedicated biological SAXS beamlines acknowledge the need to check for and avoid radiation damage.



Radiation damage in most contexts is a function of Dose (Gy = J kg⁻¹). $Dose = \frac{ftAE_{\gamma}}{\rho l}$

- flux density
- exposure time
- fraction of incident energy absorbed
- E_{γ} energy of photon
 - sample density
 - path length

Jesse Hopkins and Robert Thorne, J. Appl. Cryst. (2016) 49:880-890

ρ

Minimize:

Reduce exposure time

Decrease volume irradiated Oscillating or continuous flow Defocusing the beam

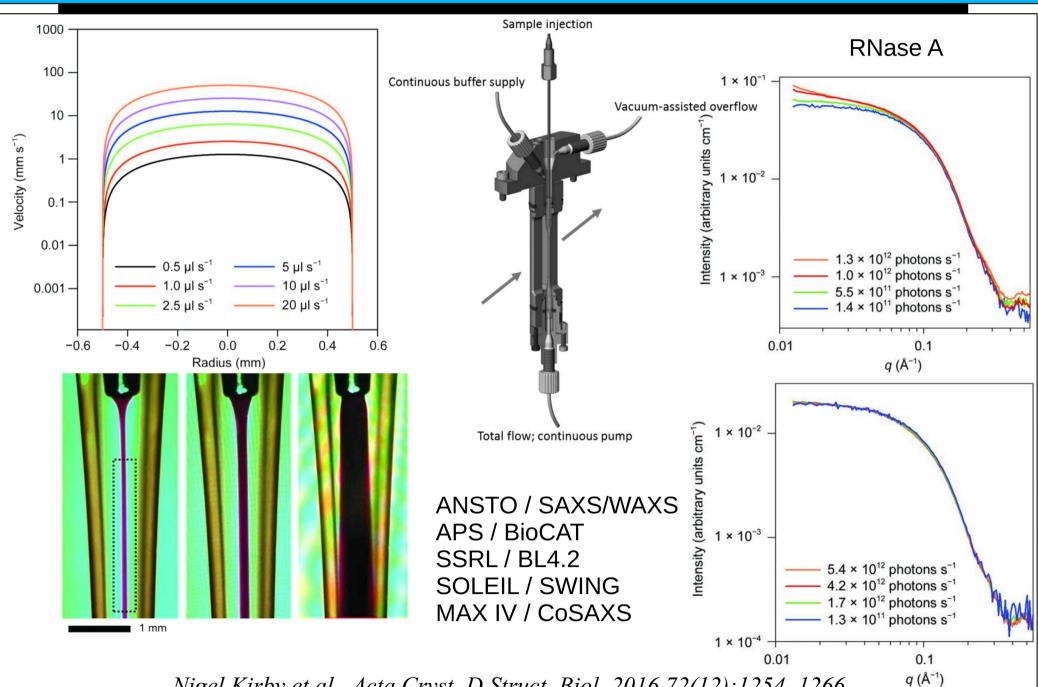
 $Dose = \frac{ftAE_{\gamma}}{ol}$

Buffer additives to competitively bind with free radicals or by inhibit aggregration

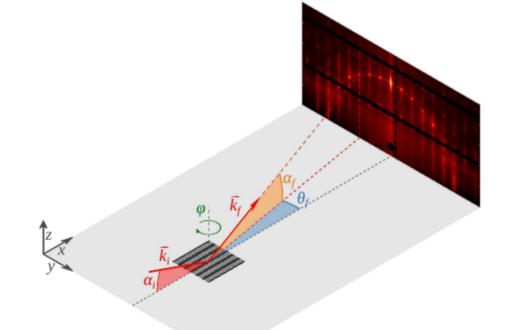
Glycerol

Cryo-SAXS

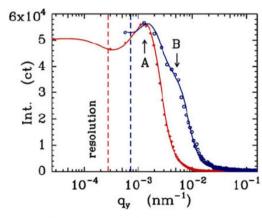
Jesse Hopkins and Robert Thorne, J. Appl. Cryst. (2016) 49:880-890

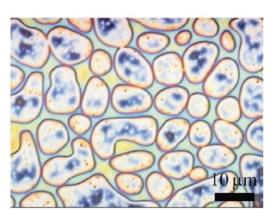


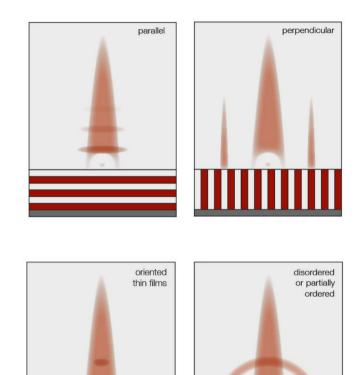
Nigel Kirby et al., Acta Cryst. D Struct. Biol. 2016 72(12):1254–1266.



Müller-Buschbaum P. (2009) A Basic Introduction to Grazing Incidence Small-Angle X-Ray Scattering. Lecture Notes in Physics, vol 776, Springer



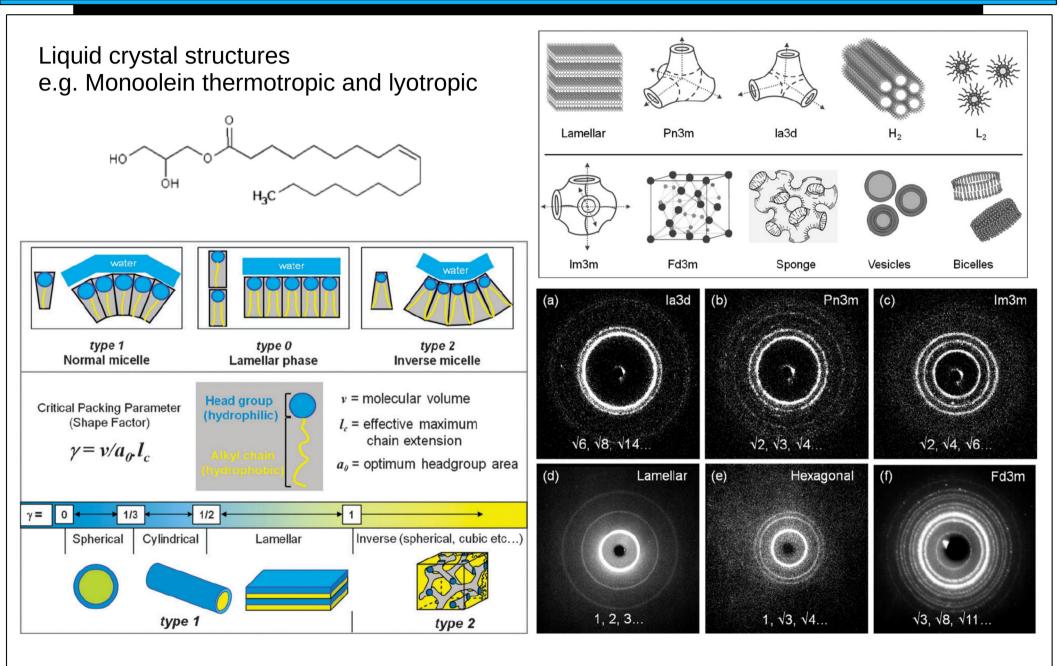




https://wiki.anton-paar.com/en/grazingincidence-small-angle-x-ray-scattering-gisaxs

Blend films of PS and PnBA "A" most prominent in-plane length

Müller-Buschbaum P., Prog. in Colloid & Polymer Sci. 2006 doi:10.1007/2882_031



C. V. Kulkarni et al. Phys. Chem. Chem. Phys. 2011, 13:3004-3021

Monodispersity revisited

Svergun – 2003

Shannon channels = $D_{max} \cdot q$ -range / π

"the number of [obtainable parameters] typically does not exceed $10\mathchar`-15$ Hub-2018

"... generally accepted that experimental SWAXS curves do not contain more than 10–30 independent data points."

Monodispersity \rightarrow maximize information content / species

Even if you purify immediately before SAXS measurements and inject each fraction or a pool of fractions, you still have a chance that the sample will either aggregate or degrade during operations

- High pressure liquid chromatography or FPLC (Fast protein liquid chromatography) on line with the SAXS cell
- Individual peaks are more likely to be monodisperse
- First use paper, available to users who could self-manage FPLC
 - *Mathew, E., Mirza, A., & Menhart, N. (2004)*. Liquid-chromatography-coupled SAXS for accurate sizing of aggregating proteins. *J. Synchrotron Rad. 11, 314-318*.
- First setup with user HPLC support
 - *David, G. & Pérez, J. (2009).* Combined sampler robot and high-performance liquid chromatography: a fully automated system for biological small-angle X-ray scattering experiments at the Synchrotron SOLEIL SWING beamline. *J. Appl. Cryst. 42, 892-900*
- Implementations (not guaranteed exhaustive)
 - ID-18 BioSAXS/APS
 - BL4.2/SSRL
 - CHESS/MacCHESS
 - SWING/SOLEIL
 - BM-29/ESRF
 - I22/Diamond
 - P12/Petra
 - SR13 ID01/Australian Synchrotron

Inline HPLC/MALS system

SWING/SOLEIL

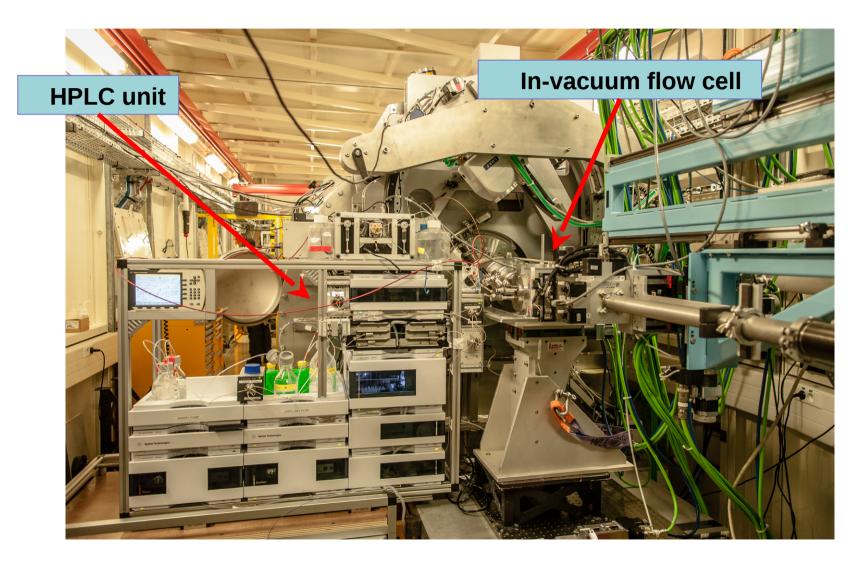
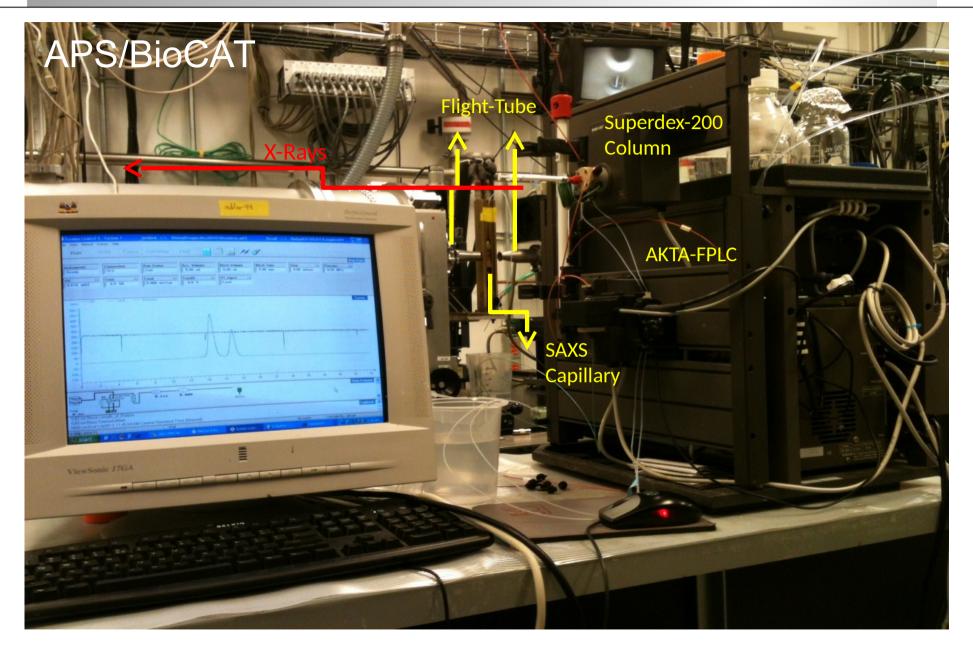


Photo credit: Javier Perez

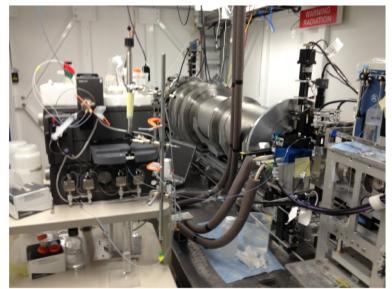


Slide Credit: Srinivas Chakravarthy

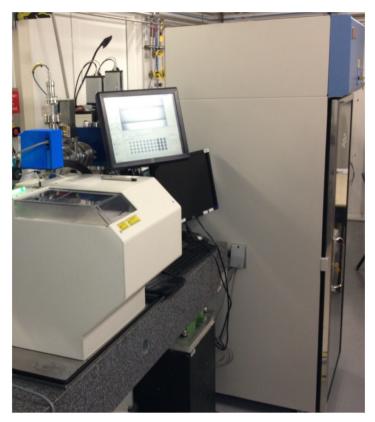
SSRL/BL4.2

- The online FPLC-SAXS system at the BioSAXS beamline BL4-2
- consists of an Akta Ettan with low volume (2.5ml) SEC columns:
 - Superdex 200
 - Superose 6
 - Or bring your own
- The system uses the same flow path as the
- regular "autosampler" setup at the beamline:
 - rapid switch-in of the FPLC system during normal data collection
 - FPLC-SAXS and "autosampler" results can be compared quickly
- sample requirement:
 - typically 50ul of 5mg/ml sample
 - each run requires 3 ml of buffer and takes roughly an hour
- Automated data analysis scripts allow easy tracking of experimental results during experiment
- More information on our website:
 - http://www-ssrl.slac.stanford.edu/~saxs/





BM29/ESRF



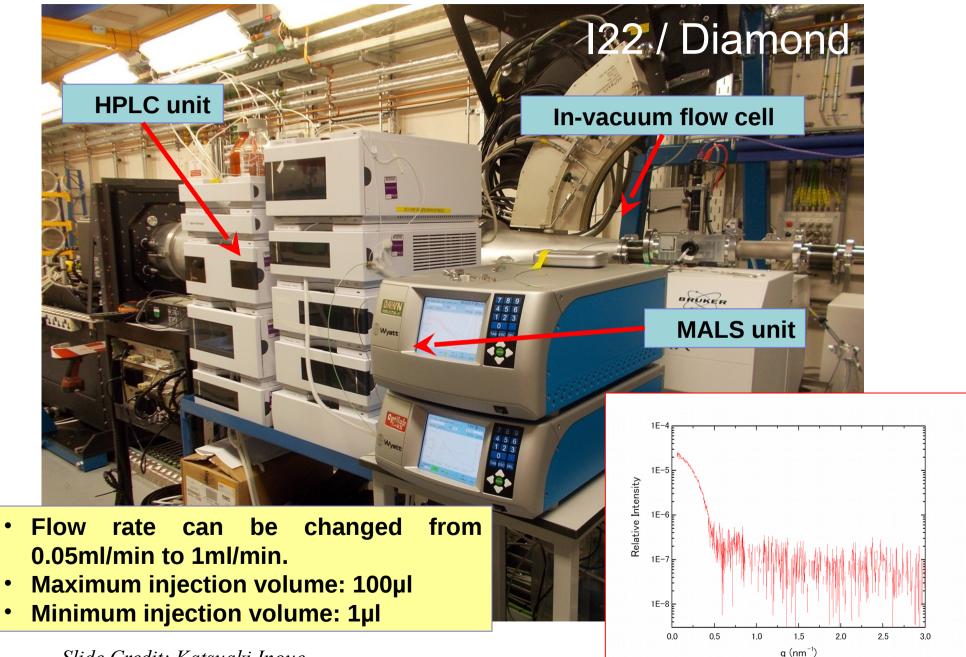
Automated switching between SEC and SC for efficient use

Integrated Sample changer and Online-SEC SEC units housed in temperature controlled cabinet (4 -25 °C)



Slide Credit: Adam Round

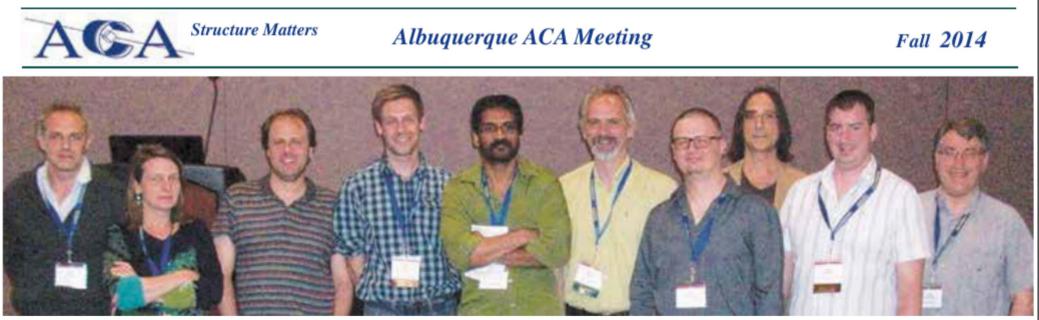




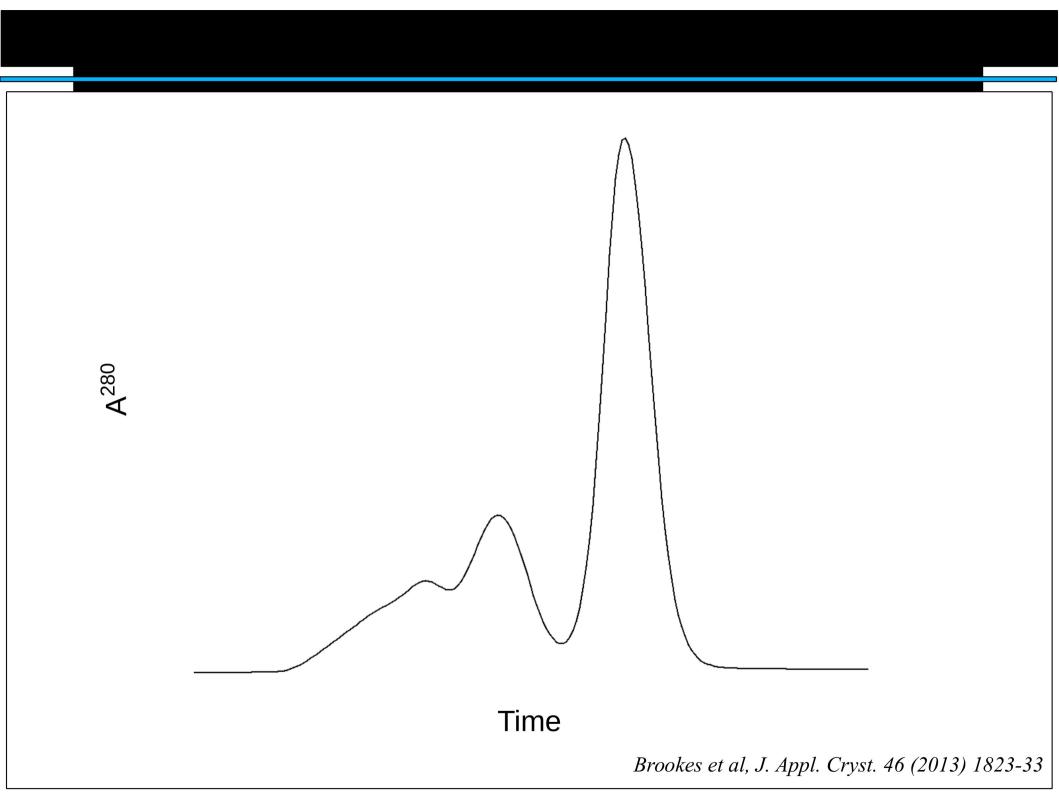
Slide Credit: Katsuaki Inoue

- Separate immediately before measuring
- Individual peaks are more likely to be monodisperse
- Now available as primary method of analysis at multiple beamlines
- Conclusion of ACA 2014 session 4.2.4 [ACA Reflexions Fall 2014]:

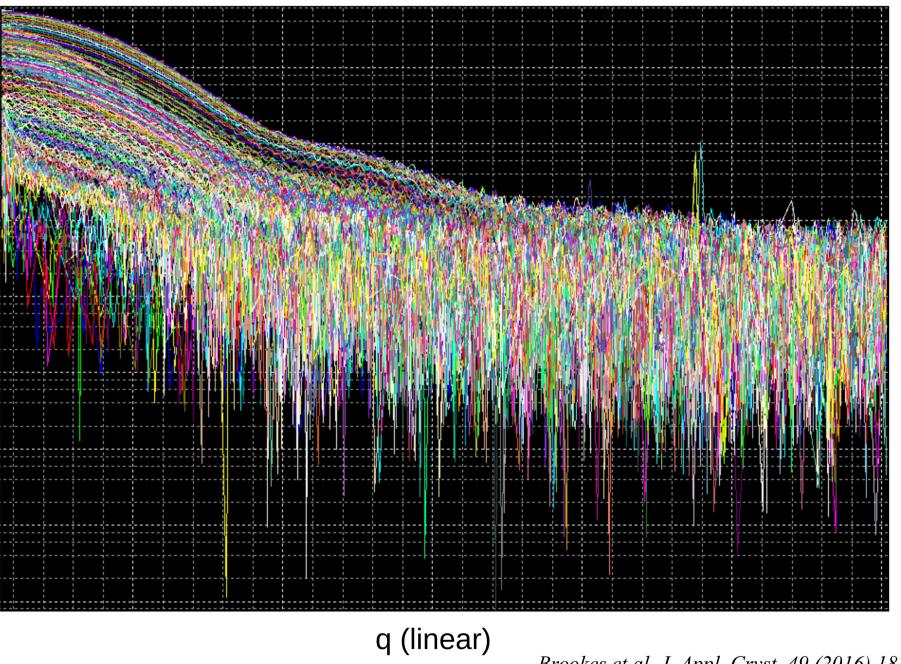
"The consensus that emerged was that SEC-SAXS may become the standard data collection strategy for biological samples, as a large number of samples that were heretofore believed to be monodisperse have been shown to be polydisperse when analyzed with online SEC-SAXS setups."



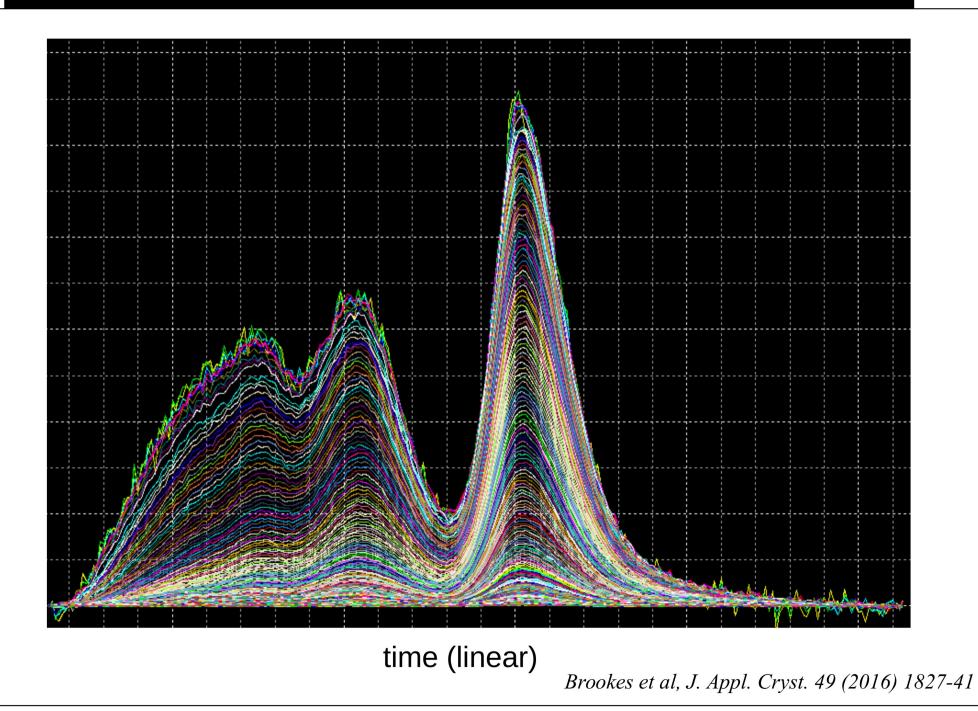
Nicolas Wolff, Sophie Zinn-Justin, Nigel Kirby, Alvin Acerbo, Srinivas Chakravarthy, Javier Pérez, Alexey Kikhney, Emre Brookes, Adam Round, David Lambright.



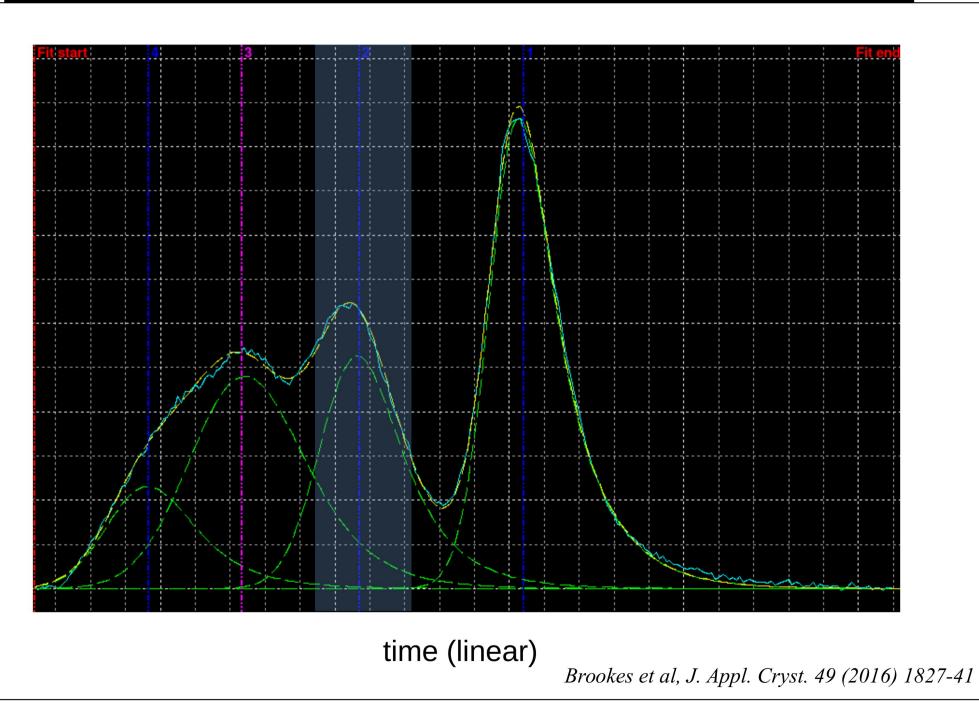
Intensity (log)

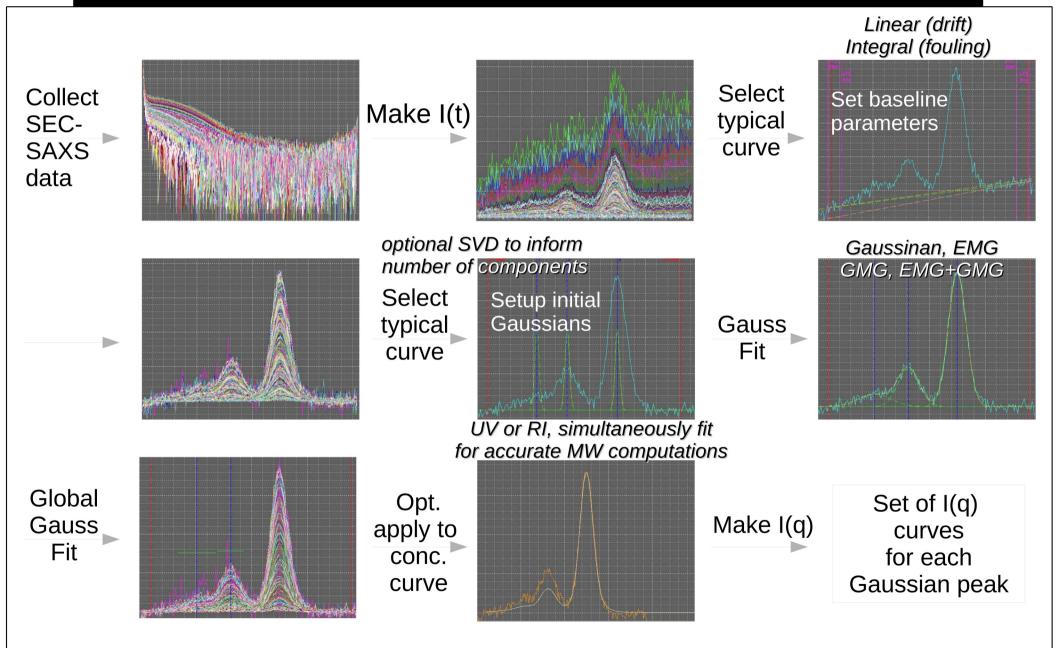


Intensity (linear)



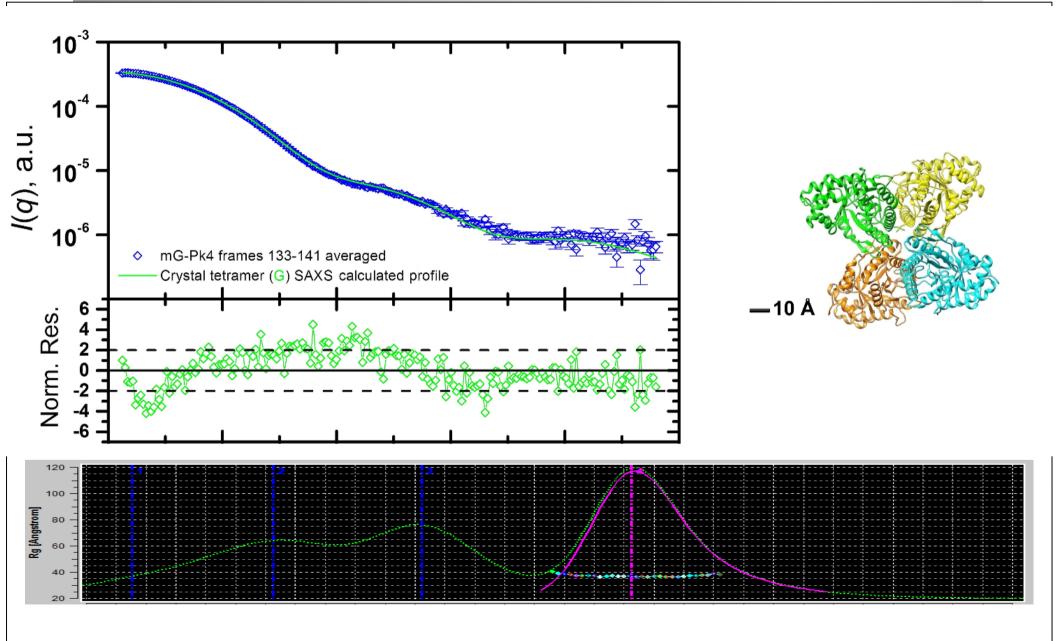
Intensity (linear)



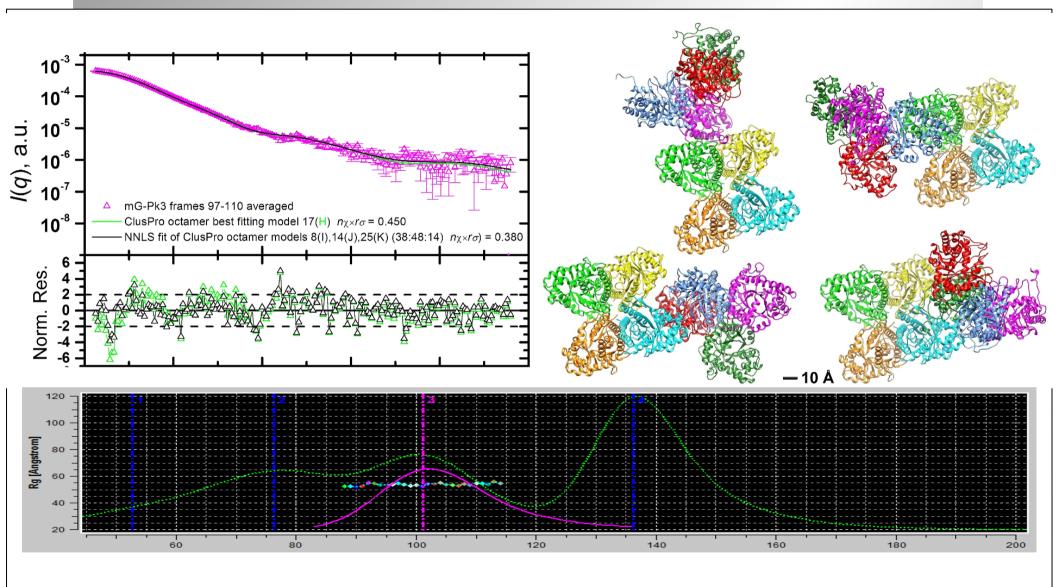


Brookes et al, J. Appl. Cryst. 46 (2013) 1823-33 Brookes et al, J. Appl. Cryst. 49 (2016) 1827-41

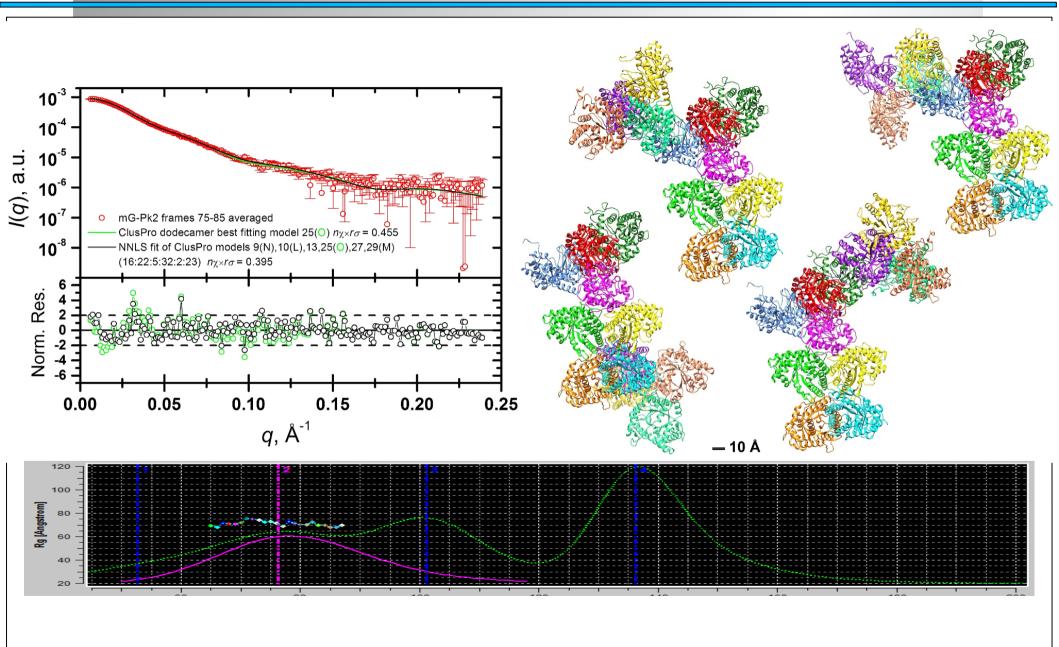
Deconvolution of Aldolase & Model

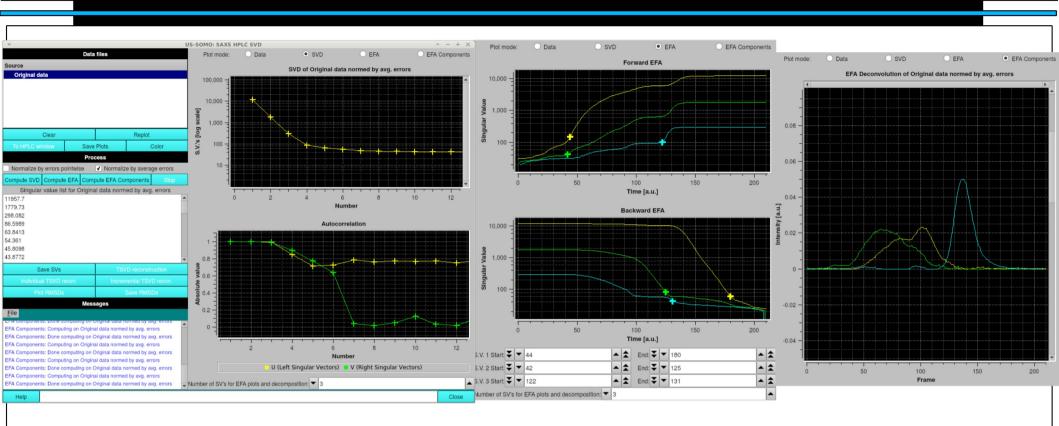


Deconvolution of Aldolase & Model

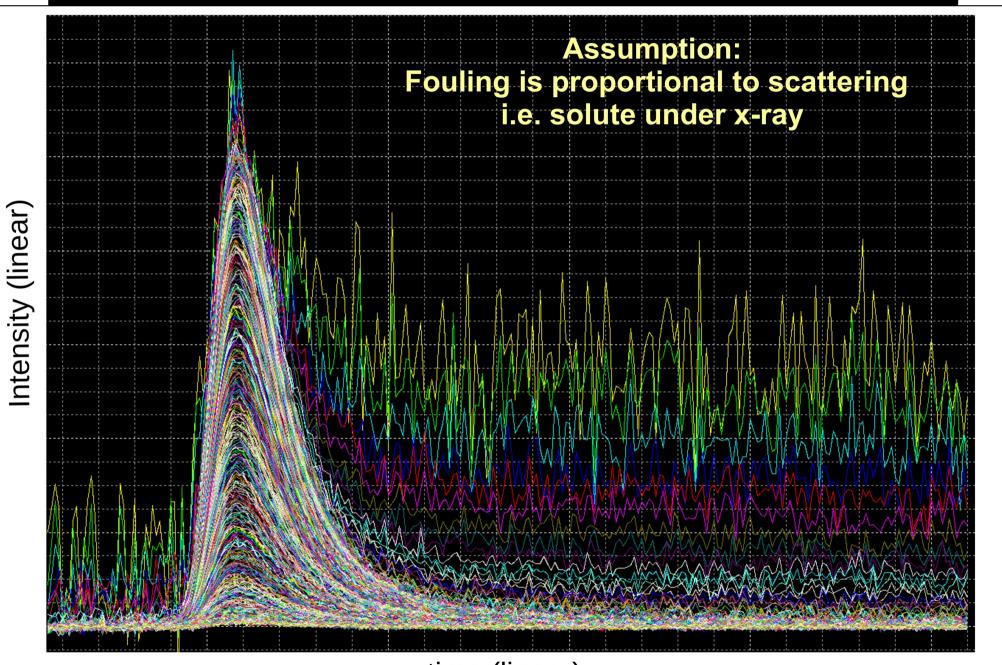


Deconvolution of Aldolase & Model



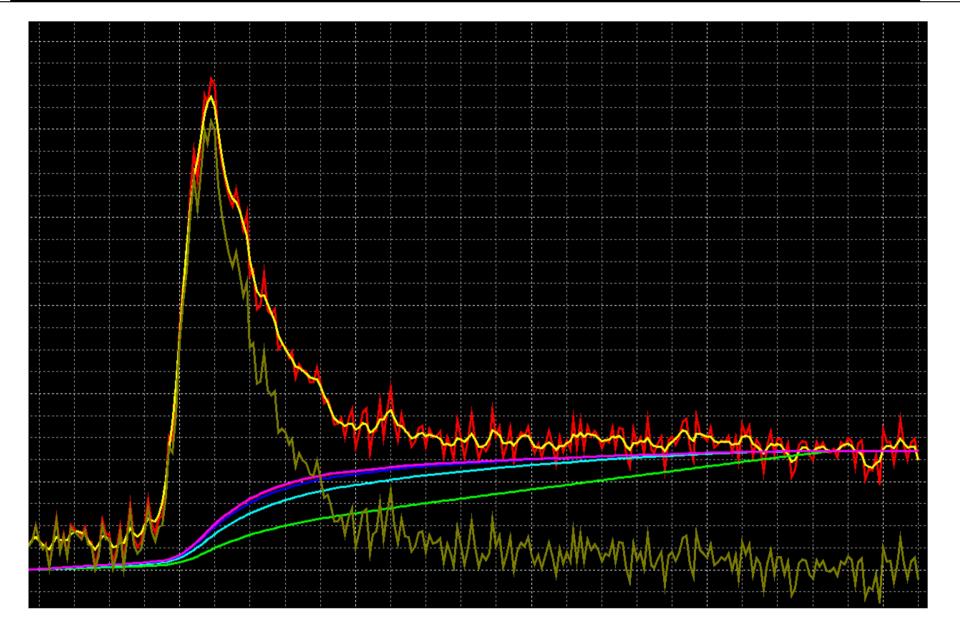


Hopkins et al. (2017) J. Appl. Cryst. 50(5) 1545-53 Meisburger et al. (2016) J. Am. Chem. Soc. 138 6506-16



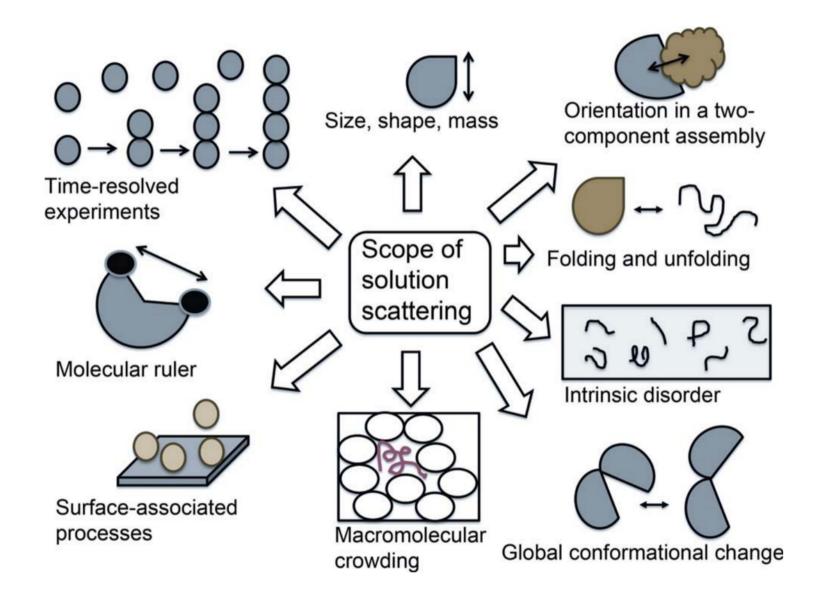
time (linear) Brookes et al, J. Appl. Cryst. 49 (2016) 1827-41





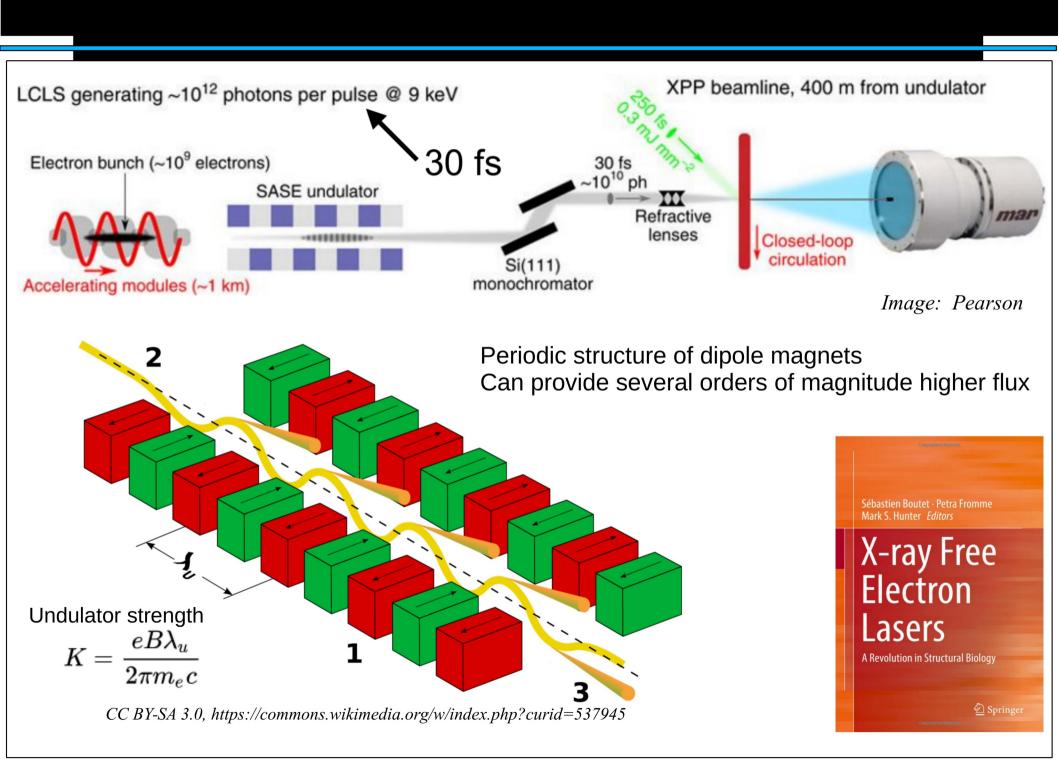
time (linear) Brookes et al, J. Appl. Cryst. 49 (2016) 1827-41

- If you have sufficient sample use SEC-SAXS for biological macromolecules
- If you have true baseline separation, excellent, you should probably be ok simply taking the peak data, but global Gaussian decomposition will use all of the data
- If you do not have true baseline separation, be very careful and you should use these techniques



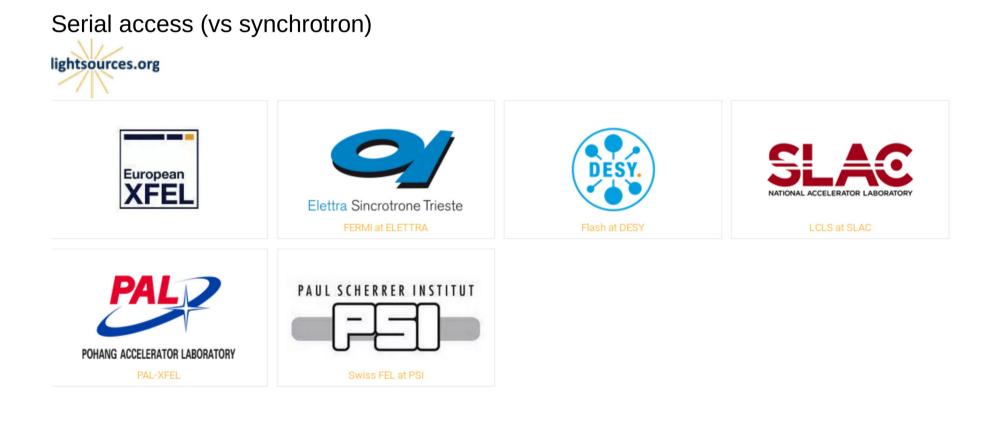
B. N. Chaudhuri. Prot. Sci. 2015 24:267-276





2 point correlations : $p(r) \rightarrow 4$ point correlations promises possibility of better 3d models Still early days.

Few XFELs instruments





Beyond Rg Bio https://small-angle.aps.anl.gov/future-courses#BeyondRgBio



National School on Neutron and X-Ray Scattering *https://neutrons.ornl.gov/nxs*





http://hercules-school.eu/



Practical courses http://embo.org/funding-awards/courses-workshops/practical-courses

Books

"La diffraction des rayons X aux très petits angles: Application a l'etude de phénomènes ultramicroscopiques":

A. Guinier (1939), Ann. de Phys., 11:12 pdf in course papers

"Small Angle Scattering":

A. Guinier and A. Fournet, (1955), in English, ed. Wiley, NY

"Small Angle X-Ray Scattering":

O. Glatter and O. Kratky (1982), Academic Press. pdf available http://physchem.kfunigraz.ac.at/sm/Software.htm

"Structure Analysis by Small Angle X-ray and Neutron Scattering": L.A. Feigin and D.I. Svergun (1987), Plenum Press. pdf available http://www.embl-hamburg.de/ExternalInfo/Research/Sax/reprints/feigin_svergun_1987.pdf

"Neutrons, X-Rays and Light, Scattering methods applied to soft condensed matter": *P. Lindner and T. Zemb Eds, (2002) Elsevier, North-Holland.*

The Proceedings of the SAS Conferences held every three years are usually published in the Journal of Applied Crystallography